

# Quality-Adjusted Price Indices Powered by AI

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**Amazon Core AI**

# Motivation

- Inflation indices are important inputs into measuring aggregate productivity and cost of living, and conducting monetary and economic policy.
- We want to contribute to the science of inflation measurement based on **quality-adjusted (hedonic)** prices.
- Main challenges today:
  1. millions of products (global trade environment);
  2. prices change quite often;
  3. extremely high turnover for some products (e.g., apparel, electronics).
- Our teams addressed these challenges to produce a method that utilizes scalable **AI and Econometrics** tools to predict quality-adjusted prices using text and image embeddings

## We want to share our findings:

- 1. Deep learning embeddings, produced by Deep Neural Networks (DNN) provide valuable input features for hedonic models.
- 2. Deep learning (utilizing DNN) leads superior price prediction compared to ML and other methods.

# Outline

- 1) Basic Price Indices
- 2) Quality-Adjusted (**Hedonic**) Price Indices
- 3) Hedonic Prices Indices Using ML and AI
  - 1) Feature Engineering from Text
  - 2) Feature Engineering from Images
  - 3) Nonlinear Price Prediction using Neural Networks
- 4) Conclusion

# Transaction-Price Quantity Index (TPQI)

- Price  $P_{jt}$  and quantity  $Q_{jt}$  for product  $j$  in period  $t$
- Transaction-Price Quantity Indices are based on **matching**:

Paasche Index: 
$$R_t^{P,M} = \frac{\sum P_{jt}Q_{jt}}{\sum P_{j(t-1)}Q_{jt}}$$

Laspeyres Index: 
$$R_t^{L,M} = \frac{\sum P_{jt}Q_{j(t-1)}}{\sum P_{j(t-1)}Q_{j(t-1)}}$$

Fisher Index: 
$$R_t^{F,M} = \sqrt{R_t^{P,M} R_t^{L,M}}$$

where the summation in the denominator/numerator is over the matching set (largest common set).

- Missing products **create biases in the matching set**.

# Need for Hedonics (Quality-Adjusted Pricing)

- To avoid biases in the **matching set**, we can predict prices of missing products in period-to-period comparisons. Relevant for product categories with high turn-over.
- In product groups like apparel, **about 50% of products get replaced** with new products **every month**.
- **Matching sets** can be non-representative of good baskets, creating systematic biases.
- **Use predicted prices, using product attributes or qualities**, instead of the missing and observed prices

# Hedonic Price Quantity Index

- **Replace prices by quality-adjusted prices**

Paasche Index: 
$$\hat{R}_t^{P,M} = \frac{\sum \hat{P}_{jt} Q_{jt}}{\sum \hat{P}_{j(t-1)} Q_{jt}}$$

Laspeyres Index: 
$$\hat{R}_t^{P,M} = \frac{\sum \hat{P}_{jt} Q_{j(t-1)}}{\sum \hat{P}_{j(t-1)} Q_{j(t-1)}}$$

Fisher Index: 
$$\hat{R}_t^{F,M} = \sqrt{\hat{R}_t^{P,M} \hat{R}_t^{L,M}}$$

- **Summation is done over the union of products that transacted in two periods**

# The Hedonic Price Model: Predictive Model for Price Using Product Features

The hedonic model is the predictive model for price given the product features:

$$\underbrace{P_{jt}}_{Y_{jt}} = P_t(\underbrace{W_{jt}, I_{jt}}_{X_{jt}}) + \epsilon_{jt},$$

where  $P_{jt}$  is the price of product  $j$  at time  $t$ ,  $X_{jt}$  are the product embedding features, and the pricing function  $x \mapsto P_t(x)$  can change from period to period, reflecting the fact that product attributes/features may be valued differently in different periods.

# What are the Features?

Query: red dress

Image



Roll over image to zoom in

Customer behavior data



3,989 customer reviews | 259 answered questions

Description

- Material - Cotton & Spandex.
- Imported
- Classic and Iconic Audrey Hepburn 50s Vintage Solid Color Swing Dress, Put on and Show Your Elegance and Charm.
- Features: Boat Neckline; Sleeveless; Full Circle Swing; Quick Access Zipper for Easy On and Off
- It's Great Choice for Daily Casual, Wedding , Ball, Party, Banquet and Other Occasion.
- [Size Chart] PLEASE Make Sure Your Measurements and Compare to the Size Chart From the picture on the left side or in the Following Description.
- Hand Wash Carefully,Low Temperature for Washing,Can not High Temperature Ironing, Line Dry

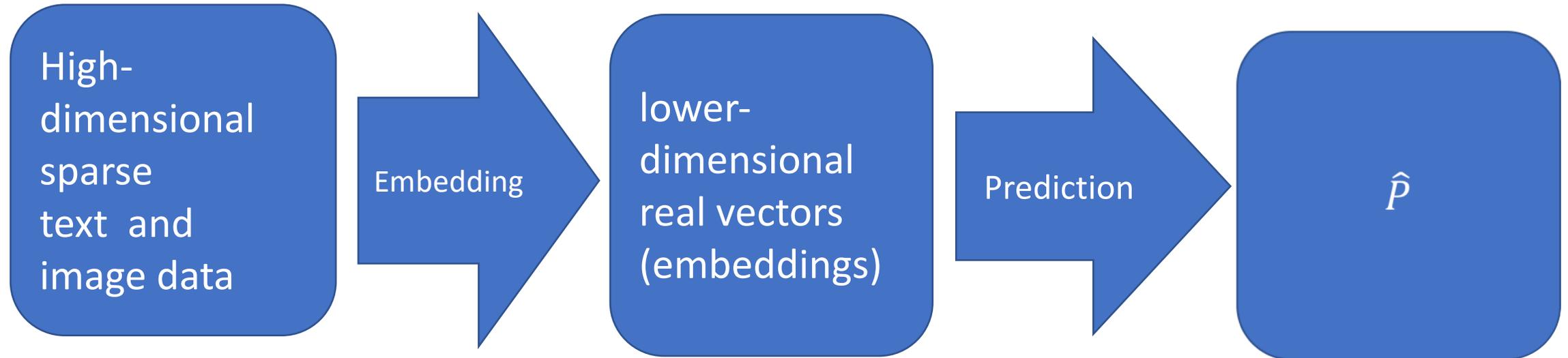
$X \in \mathbb{R}^d$

Title

Anni Coco

Anni Coco Women's Classy Audrey Hepburn 1950s Vintage Rockabilly Swing Dress

# The Process: Embeddings and Predictions



- **Embedding** is done by Deep Learning (Neural Network) methods:
  - a) Text ( $W$ ) : ***ELMo (Bert, W2Vec)***
  - b) Images ( $I$ ) : ***ResNet (AlexNet, GoogLeNet)***
- **Prediction** is done again by Neural Networks (other regression methods).

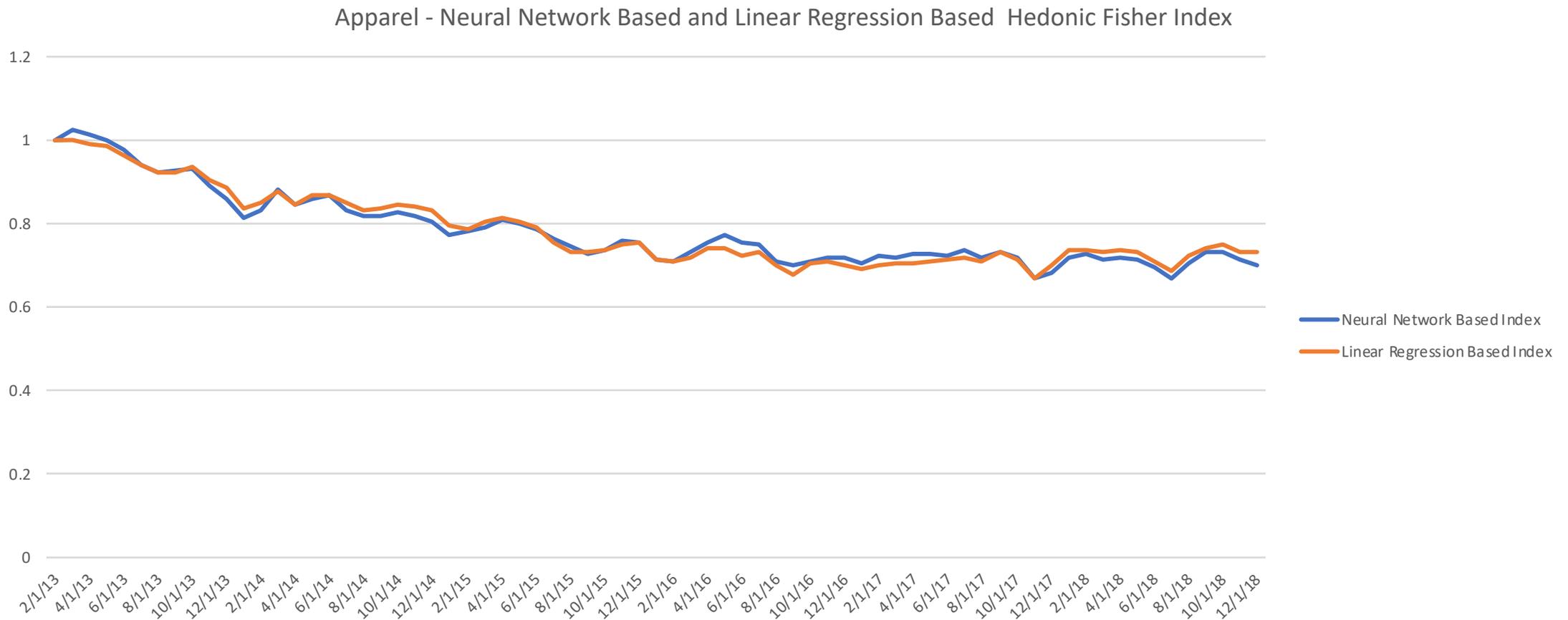
# The Benefits of Text and Image Features in Predicting Prices/Hedonic Regression

- Using only conventional features in linear regression gives  **$R^2$  for predicting log-price around 30%**.
- Using  **$W$**  and  **$I$**  features in **Linear Regression** gives  **$R^2$  about 50%**.
- Using  **$W$**  and  **$I$**  features plus **Random Forest** brings  **$R^2 = 60-65%$** .
- Using  **$W$**  and  **$I$**  features plus **Neural Networks (NN)** brings  **$R^2 = 75-90%$** .
- All  $R^2$  results are out-of-sample.

# Performance Across Product Categories Varies

- **Best Cases:** Apparel, Electronics, Baby; Neural Network R-square > 75%
- **Tough Cases:** Toys, Books, Shoes; Neural Network R-square ranges from 40 to 60 %

# (Preliminary) Empirical Result: Amazon Hedonic Index for Apparel Product Group



**The Index is Chained Month-over-Month**

- For comparison, the non-hedonic Fisher index *decreases much more* over the period 2013-2018.
- The simple hedonic index, that is based on simple catalogue information, also decreases much more than the hedonic index (but less drastically than the non-hedonic Fisher index).
- *N.B. The results are not representative of the general inflation/deflation patterns in the U.S. At best they provide a data-point in the e-commerce subsector of the overall retail sector.*

# Hits and Misses: Examples



 Carhartt Women's Sherpa Lined Sandstone Sierra Jacket (Regular and Plus Sizes)  
★★★★☆ 1,162 customer reviews | 143 answered questions

Price: \$107.34 - \$222.90 & Free Return on some sizes and colors

Fit: As expected (75%)

Size:  
Select Size Chart

Color: Black



- 100% Cotton
- Imported
- Zipper closure
- Machine Wash
- Zip-front jacket featuring attached three-piece hood and ribbed-knit storm cuffs
- Lined in faux shearling
- Pockets at chest and waist
- Princess seaming at back

AMOJI  
Amoji Unisex House  
Slipper  
> Shop now



Amoji Lined Slipper Clog  
House Home  
★★★★☆ 140

Ad feedback  
🗨

NN and Linear Regression gave accurate predictions for this product about 100 (with Linear Regression underpredicting the price).

# Hits and Misses: Examples

Contemporary & Designer › Clothing › Dresses › Casual



[CG Chris Gelin](#)

CG Chris Gelin Women's Silk Brocade Letter Print Dress

Price: ~~\$2,395.88~~ & **FREE Shipping**. [Details](#)  
[FREE Returns](#)

**Note:** Signature required upon delivery due to high value of this item. [Details](#) ▾

**Size:** 4

**Color:** Navy Multi

- 54% Silk, 46% Polyester; Print Combo: 100% Silk; Combo: 100% Cotton; Lining: 100% Silk
- Made in US
- Dry Clean Only
- Cruising around custom rose gold buttons
- Floor length

**New (1)** from ~~\$2,395.88~~ & **FREE shipping**. [Details](#)



[Vitamin C  
with  
Echinacea](#)  
\$9.26



[Elderberry  
Complex](#)  
\$9.99

NN and Linear Regression underpredicted the price. **NN predicts the price of 230;** **Linear Regression predicts the price of 90.**

This CG designer dress is a hard item to predict: many other items by the same brand are priced at around 200. Do the models miss some attributes? (e.g., custom-made rose gold buttons).

# Dynamic Approach: Using Leads and Lags To Predict Missing Prices

- We can also use leads and lags of prices to predict missing prices . A simple motivation can be given by considering a model where (approximately):

$$P_{jt} = P_{jt}(X_j, U_j)$$

- Where  $U_j$  is the latent unobserved quality characteristics. Assume the price is monotonically increasing in the latent quality. Then conditioning on the previous and future values of  $P_{jt}$  is equivalent to conditioning on  $U_j$ .
- In constructing the index, either a leads or lag is always available, since the product  $j$  has transacted at least in one period.

# The Benefits of Dynamic Model

- Using only leads and lags brings  **$R^2$  for predicting log-price around 93%**. Using  **$W$**  and  **$I$**  features in addition only adds about **.5-1%** in fit
- While the dynamic approach can be good with the **Month-over-Month** chaining (still biases may occur, since predictions are based on the matching set of products).
- It may perform poorly with the **Year-over-Year** chaining (since the set of surviving products to train the dynamic predictive model can be small and biased). By contrast, hedonics performs well with the YoY chaining.
- Dynamic Approach gives results very close to non-hedonic Fisher index (showing more drastic deflation over 6 years).

# Technical Details of Feature Engineering

Query: red dress

Image



Roll over image to zoom in

Customer behavior data



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Description

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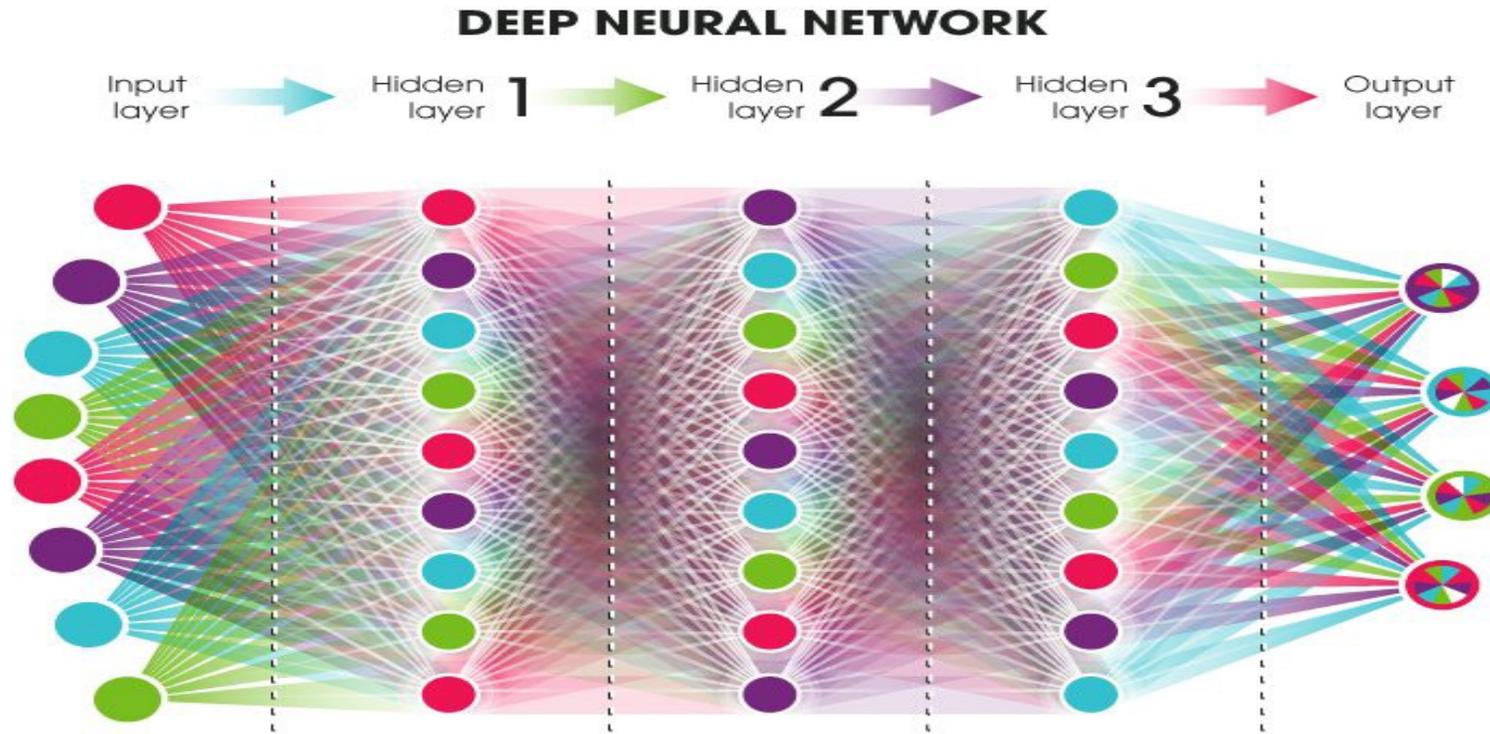
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# Features are created by (Deep) Neural Nets



# Word2vec

In summary, dictionary  $V$  consists of binary words, and embeddings  $W$  are generated by applying a rank  $m \ll d$  matrix to produce embeddings:

$$\underbrace{W}_{m \times d} = \underbrace{w}_{m \times d} \underbrace{V}_{d \times d}.$$

Given a sequence of  $K$  words,  $\{V_{j,m}\}_{j=1}^K$ , indexed by  $m$ , we have a middle word  $V_{i,m}$  whose identity we have to predict from the surrounding words  $\{V_{j,m}\}_{j=1}^{K-1}$ .

Collapse the embeddings for context words by a sum,

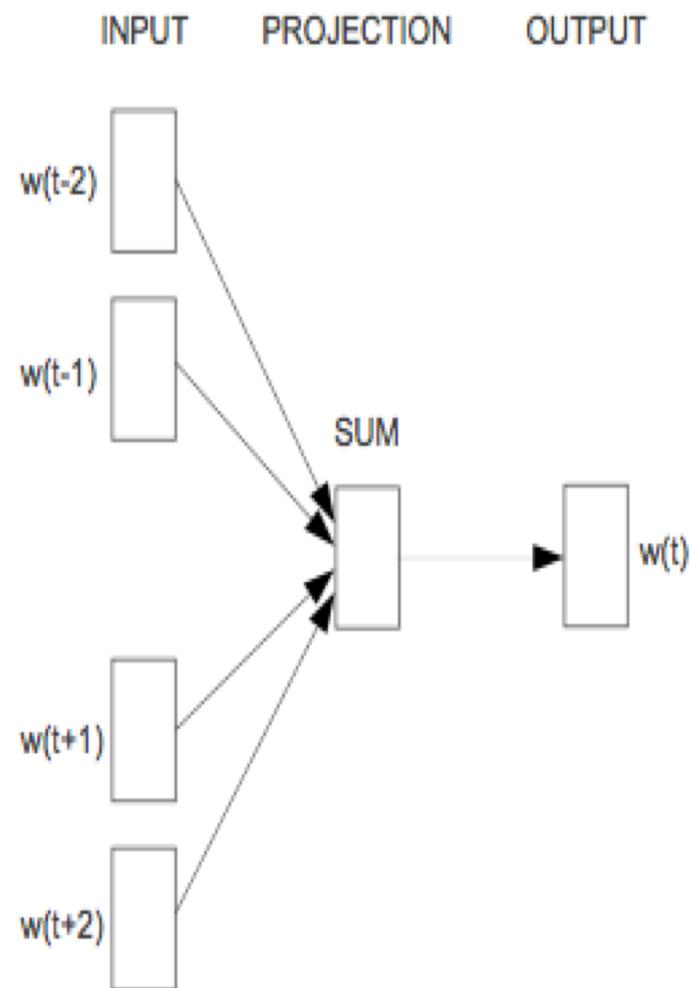
$$\bar{W}_m = \sum_j W_{j,m}.$$

This reflects the assumption that the context words are exchangeable, an assumption that simplifies the model, but is clearly very strong.

The probability of middle word  $V_{i,m}$  being equal to the  $k$ -th word in the dictionary is modeled as

$$P(V_{i,m} = v_u \mid \{V_{j,m}\}_{j \in \{1, \dots, K-1\} \setminus i}; \pi, w) = Z_u = \frac{e^{\pi'_u \bar{W}_m}}{\sum_{l=1}^d e^{\pi'_l \bar{W}_m}},$$

where  $\pi_k$  are conformable parameter vectors, describing the choice probability.



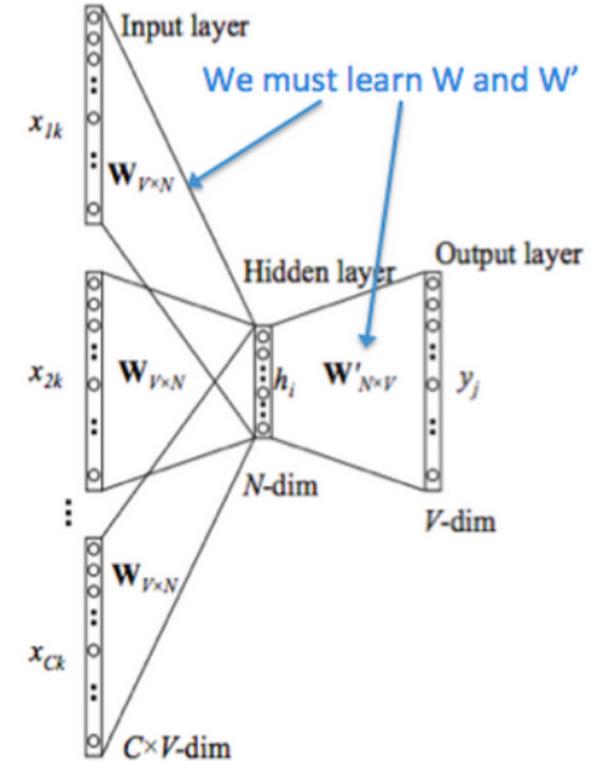
**CBOW**

# Word2vec

The key parameters are the parameters of multinomial logistic distribution:  $\pi = (\pi'_1, \dots, \pi'_d)$  and the parameters  $w$  of the embedding hidden layer.

The are jointly estimated using the maximum quasi-likelihood method:

$$(\hat{\pi}, \hat{w}) = \arg \max_{w, \pi} \sum_m \left( \begin{array}{l} 1(V_{i,m} = V_k) \log P(V_{i,m} = V_k | \{W_{j,m}\}) \\ + 1(V_{i,m} \neq V_k) \log P(V_{i,m} \neq V_k | \{W_{j,m}\}) \end{array} \right).$$



# Word Embeddings: Examples

womens	0.387542	0.03051	-0.19703	0.179724	-0.222901	-0.606905	0.306091	-0.597467
mens	0.758868	0.372418	0.370116	0.706623	-0.124954	0.5088	0.106177	0.208935
clothing	0.149283	0.5161	-0.027684	0.218484	-0.851416	-0.409885	0.386088	0.170605
shoes	1.323812	-0.358704	-0.007683	-0.552144	0.011261	0.365239	0.228273	-0.565655
women	0.601477	-0.045845	-0.099481	0.010576	-0.096852	-0.605281	0.25606	-0.550759
girls	0.417473	-0.005265	-0.40939	-0.531189	-1.31938	-0.034746	-0.940507	-0.361215
men	0.778298	0.406613	0.426292	0.534272	-0.056103	0.51756	0.107846	0.245275
boys	0.896637	-0.016821	-0.001602	-0.181901	-1.313441	0.449006	-0.828408	0.52121
accessories	0.86825	-0.378385	-1.247708	1.541265	0.323952	0.282909	-0.491176	0.081314
socks	0.27636	0.354296	0.185734	0.301311	-0.643142	-0.021945	0.320751	0.240676
luggage	0.796763	1.749548	-2.30671	-0.559585	0.03054	0.921458	0.417333	0.313436
dress	0.282053	0.233192	0.043318	0.174759	-0.50114	-0.381047	0.297995	-0.026033
baby	0.346065	-0.550016	-1.136202	-0.043899	-2.004979	0.689747	-1.091575	0.009901
jewelry	-0.315784	0.347808	-0.308736	0.878713	-0.766016	1.124318	-0.079883	-2.039485
black	0.427496	0.030204	-0.019082	0.224096	-0.162242	-0.325359	0.170407	-0.172714
boots	1.009074	-0.30359	0.03197	-0.334004	-0.095679	0.111328	0.11769	-0.51878
shirts	0.444152	0.452918	0.393656	0.517929	-0.531462	0.099621	0.146202	0.204338
shirt	0.328998	0.421561	0.226565	0.455649	-0.700352	0.067224	0.106364	0.233862
underwear	0.230821	0.490978	0.226338	0.202376	-0.774363	0.004693	0.228712	0.310215

# Word2Vec Embeddings have interesting properties

$\text{Word2Vec}(\text{"handbag"}) + \text{Word2Vec}(\text{"men"}) - \text{Word2Vec}(\text{"woman"})$   
 $\approx \text{Word2Vec}(\text{"briefcase"})$

$\text{Word2Vec}(\text{"tie"}) + \text{Word2Vec}(\text{"woman"}) - \text{Word2Vec}(\text{"men"})$   
 $\approx \text{Word2Vec}(\text{"pashmina"}), \text{Word2Vec}(\text{"scarf"})$

- Distance is the Cosine Distance = Euclidian distance after normalizing vector norms to unity
- Embeddings for Title and Product Description are obtained by summing of the individual words

# ELMO exploits the context more

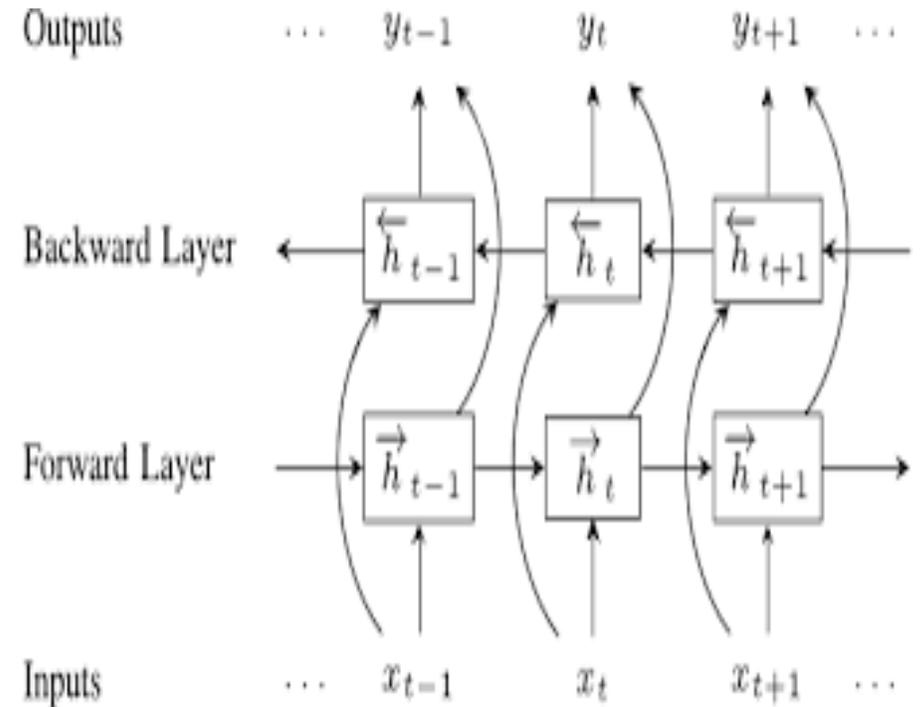
**ELMO Embeddings.** The ELMO algorithm uses the ideas of the Shannon game, where we guess the next word in the sentence  $m$ , i.e.

$$P[V_{k,m} | V_{1,m}, \dots, V_{k-1,m}; \theta]$$

and also uses the reverse guessing as well:

$$P[V_{k,m} | V_{k+1,m}, \dots, V_{K_m,m}; \theta]$$

Recursive neural networks with a single or multiple hidden layers are used to model these probabilities. Parameters are estimated using quasi maximum log-likelihood methods, where the forward and backward quasi-likelihoods are added together.



# ResNet50 Image Embedding

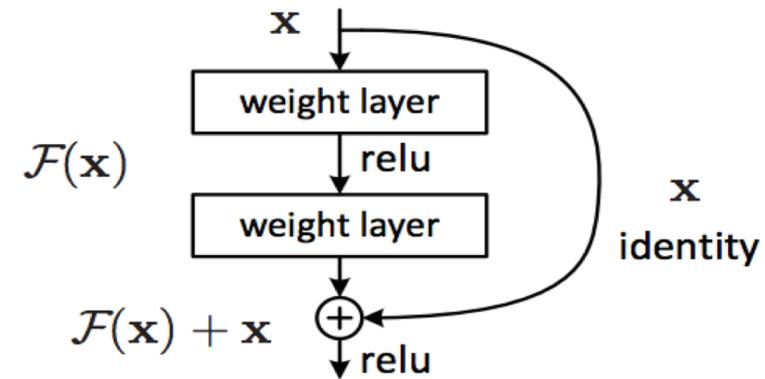
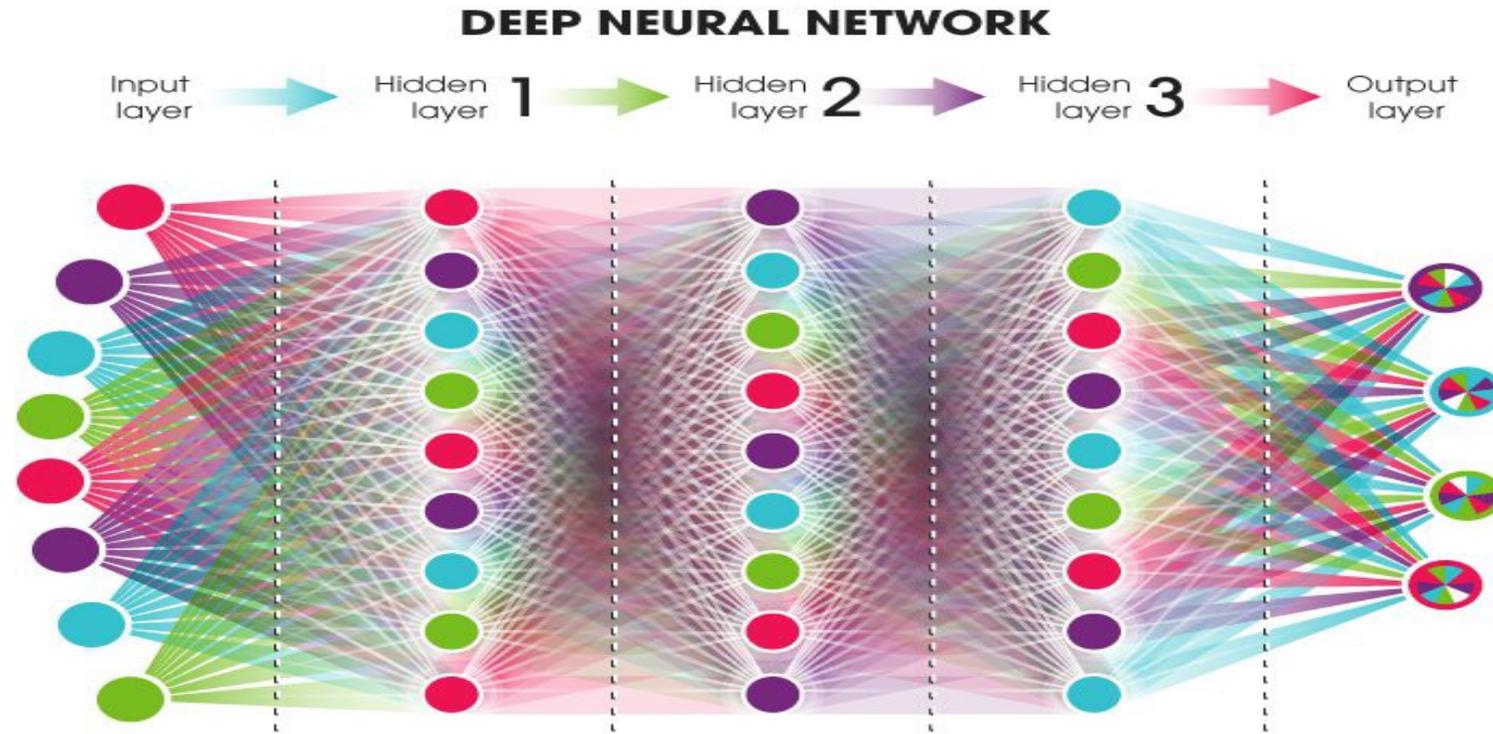


Figure 2. Residual learning: a building block.

a repeated composition of  
the superposition of the linear (identity map)  
with a nonlinearly generated layer

```
('Predicted:', [(u'n03450230', u'gown',  
0.4549656), (u'n03534580', u'hoopskirt',  
0.3363025), (u'n03866082', u'overskirt',  
0.20369802)])
```

# Predictions are created by Neural Nets with just several layers



# Conclusions

- Inflation indices are important inputs into measuring productivity and cost of living, and monetary and economic policy
- Our work addresses the *methodological challenges* in measuring inflation via hedonic approaches that arise due to
  - millions of products, with rapidly changing prices;
  - extremely high turnover for some product groups;
  - unstructured product attributes (title, product description, images).
- We do so by building hedonic price indices, which utilize
  - modern scalable computation that handles large amount of data
  - modern, open-source ML and AI tools to predict missing prices using product attributes.